

4.0 Reviewing Exponents

Reviewing Exponents

Exponential Notation:

Also known as powers.

Tells you how many times to multiply a base by itself.

Ex:

$$\begin{array}{ccc} \text{Exponent} & & \text{Power} \\ & \swarrow & \nwarrow \\ & 2^4 = 16 & \\ & \nearrow & \\ \text{Base} & & \end{array}$$

$$2^4 = 2 \cdot 2 \cdot 2 \cdot 2$$

$$\therefore a^n = \underbrace{a \cdot a \cdot a \cdot \dots \cdot a}_{n \text{ times}} \quad \text{where } n \geq 1$$

Negative Exponents:

The sign of the exponent changes when you find the reciprocal (flip a fraction) of the base.

Ex:

$$2^{-3} = \frac{1}{2^3} \quad \text{or} \quad \left(\frac{4}{5}\right)^{-1} = \frac{5}{4}$$

Try it:

$$\begin{aligned} 1) \ 5^{-2} &= \\ &\frac{1}{5^2} = \\ &\frac{1}{25} \end{aligned}$$

$$\begin{aligned} 2) \ \left(\frac{2}{3}\right)^{-2} &= \\ &\left(\frac{3}{2}\right)^2 = \\ &\left(\frac{3}{2}\right)\left(\frac{3}{2}\right) = \\ &\frac{9}{4} \end{aligned}$$

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Review of the Rules

Rule	Conditions	Example
1) $a^1 = a$	None	$5^1 = 5$
2) $a^0 = 1$	$a \neq 0$	$5^0 = 1$
3) $a^m \cdot a^n = a^{m+n}$	$a \neq 0$	$2^3 \cdot 2^4 = 2^{3+4} = 2^7$
4) $\frac{a^m}{a^n} = a^{m-n}$	$a \neq 0$	$\frac{3^5}{3^2} = 3^{5-2} = 3^3$
5) $(ab)^m = a^m b^m$	$a \neq 0, b \neq 0$	$(2 \cdot 3)^5 = 2^5 \cdot 3^5$
6) $\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$	$a \neq 0, b \neq 0$	$\left(\frac{10}{5}\right)^2 = \frac{10^2}{5^2}$
7) $(a^m)^n = a^{m \cdot n}$	$a \neq 0$	$(2^3)^4 = 2^{3 \cdot 4} = 2^{12}$
8) $a^{-m} = \frac{1}{a^m}$	$a \neq 0, m \geq 0$	$5^{-2} = \frac{1}{5^2} = \frac{1}{25}$
9) $a^{\frac{1}{n}} = \sqrt[n]{a}$	$a \geq 0$	$8^{\frac{1}{3}} = \sqrt[3]{8} = 2$

*We will look at the last rule more tomorrow.