

## 4.0 Reviewing Radicals

### Reviewing Radicals

First the vocabulary:

$$n\sqrt{a}$$

$n = \text{index}$

$a = \text{radicand}$

$\sqrt{\quad} = \text{radical}$

\*When the index is 2, we don't bother writing it.

Finding the radical of a number is like applying a fractional exponent to base, where the base of the fraction is equal to the index of the radical.

For example:

$$\sqrt[2]{16} = 16^{\frac{1}{2}} = 4$$

$$\sqrt[3]{8} = 8^{\frac{1}{3}} = 2$$

Of course, this works both ways!

Try it:

$$1) 81^{\frac{1}{4}} =$$

$$\sqrt[4]{81} =$$

3

$$2) 125^{-\frac{1}{3}} =$$

$$\frac{1}{125^{\frac{1}{3}}} =$$

$$\frac{1}{\sqrt[3]{125}} =$$

$\frac{1}{5}$

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### Solving

Recall:

To solve  $x^2 = 36$ , we would square root both sides and get  $x = \pm 6$ .

$$x^2 = 36$$

$$\sqrt{x^2} = \sqrt{36}$$

$$x = \pm 6$$

The same theory applies when you have a different exponent.

$\therefore$  To solve for a base:

To Solve This:	Do this to both sides:
$x^2$	$\sqrt{\quad}$ or $\frac{1}{2}$
$x^3$	$\sqrt[3]{\quad}$ or $\frac{1}{3}$
$x^4$	$\sqrt[4]{\quad}$ or $\frac{1}{4}$
$\vdots$	$\vdots$

To solve for an exponent:

Try to re-write the equation so that you have the same base on both sides (guess and check - for now).

Rule:

If  $c^u = c^v$ , then  $u = v$ .

Ex:

$$\begin{aligned} 1) \quad & 2^x = 8 \\ & 2^x = 2^3 \\ & x = 3 \end{aligned}$$

$$\begin{aligned} 2) \quad & 4^x = 16 \\ & 4^x = 4^2 \\ & x = 2 \end{aligned}$$