

## Equivalent Solids

- If 3-dimensional shapes have the same volume, they are said to be EQUIVALENT.

## Measurements of Solids

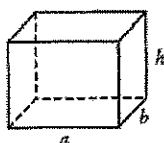
- Side Lengths
- Lateral Area
- Surface Area
- Volume

## Comparing Equivalent Rectangular

Prisms

	a (cm)	b (cm)	h (cm)	Volume	Area (cm <sup>2</sup> )
Prisme 1	64	1	1	64	258
Prisme 2	32	2	1	64	196
Prisme 3	16	2	2	64	136
Prisme 4	8	4	2	64	112
Prisme 5	4	4	4	64	96

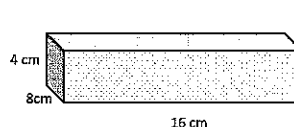
Which prism has the largest area??



## Rule #3

- Of all equivalent solids with the same number of faces, the **regular solid** will always have the **smallest surface area**

Which would have the smallest surface area?  
Find Volume and Surface Area to Verify

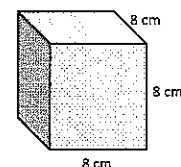


$$V = 8 \times 4 \times 16$$

$$= 512 \text{ cm}^3$$

$$A_s = 2(4 \times 8) + 2(4 \times 16) + 2(8 \times 16)$$

$$= 448 \text{ cm}^2$$



$$V = 8^3$$

$$= 512 \text{ cm}^3$$

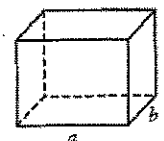
$$A_s = 6(8)^2$$

$$= 384 \text{ cm}^2$$

## Comparing Rectangular Prisms with Same Area

	a (cm)	b (cm)	h (cm)	Area (cm <sup>2</sup> )	Volume (cm <sup>3</sup> )
Prisme 1	6	6	1	96	36
Prisme 2	6	4.5	2	96	54
Prisme 3	6	4	2.4	96	57.6
Prisme 4	3	3	6.5	96	59.5
Prisme 5	4	4	4	96	64

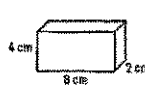
Which prism has the largest volume??



"Flip it"

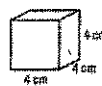
- Of all solids with the same number of faces and the same surface area, the **regular solid** will have the **greatest volume**

Find the Surface Area and Volume



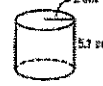
$$V = 64$$

$$A = 112$$



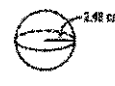
$$V = 64$$

$$A = 96$$



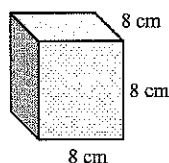
$$V = 64$$

$$A = 89.2$$



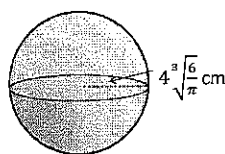
$$V = 64$$

$$A = 77.3$$



$$V = 512$$

$$A_s = 384$$



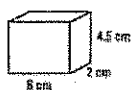
$$V = 512$$

$$A_s = 309.5$$

Rule #4

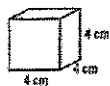
- Of all equivalent solids, the one with the **greatest number of faces** will always have the **smallest surface area**

Find the Surface Area and Volume



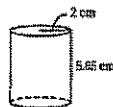
$$A_s = 96$$

$$V = 54$$



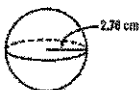
$$A_s = 96$$

$$V = 64$$



$$A_s = 96$$

$$V = 71$$



$$A_s = 96$$

$$V = 88$$

"Flip it"

- Of all solids with the same surface area, the **one with the most faces** will have the **greatest volume**