|  | Group |  |  |
| ---: | :---: | :---: | :---: |
| Graph Theory Basics | $1,2,8$ | 10 |  |
| Euler Paths and Circuits | $3,4,5$ | 6 |  |
| Hamiltonian Paths and Circuits | 6,7 | 4 |  |
| Optimal Trees | 8 | 4 |  |
| Optimal Path | 9 | 4 |  |
| Critical Path | 10 | 4 |  |
| Chromatic Number | 11 | 4 |  |

## Graph Theory Assignment

## All work on this assignment must be your own.

1. Draw a graph containing at least 5 vertices, at least 8 edges (including one set of parallel edges and one loop).
2. Using your graph above:
a. identify a simple path
b. identify a path that is not simple
c. identify a simple circuit
d. identify a circuit that is not simple.
3. Create a graph that contains an Euler Path, and identify the Euler Path in the graph.
4. Create a graph that contains an Euler Circuit and identify the Euler Circuit
5. Create a graph that does not contain an Euler Path or an Euler Circuit.
6. Create a graph that contains a Hamiltonian Path.
7. Create a graph that contains a Hamiltonian Circuit.
8. Create a graph that contains at least 6 vertices and at least 9 edges. Include weights on the edges. Now create a tree of minimum value from your graph.
9. Draw a graph containing at least 5 vertices and at least 8 edges where the path of minimum value from $A$ to $C$ is 16 .
10. Complete the table below to create a scenario in which the minimum time it takes to complete the task is $\mathbf{2 5}$ days. Create a graph from the table and verify the minimum time.

| Step | Time <br> (days) | Prior Steps |
| :---: | :---: | :---: |
| A |  | None |
| B |  |  |
| C |  |  |
| D |  |  |
| E |  |  |
| F |  |  |
| G |  |  |
| H | None |  |

11. Create a graph that has a chromatic number of 4.
